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be conservative, or even volume-

classes of maps

$$(\textbf{A}\textbf{A}) \quad \big(h_1^{-1}\cdots h_m^{-1}\big)t\,(h_m\cdots h_1)t$$

$$(\textbf{E}\textbf{A}) \quad \big(h_1^{-1}\cdots h_m^{-1}\big)e_{m+1}(h_m\cdots h_1)t$$

$$(\textbf{EE}) \quad \big(th_1^{-1}\cdots h_m^{-1}\big)e_{m+1}(h_m\cdots h_1t)e_0$$

where  $h_i$  represents a Hénon transformation in the form (2)  $\alpha$ 

**Theorem 2** (cf. [9, Corollary 2.3] or [15, Theorem 4.4]). Two reduced words  $g_m \cdots g_1$  and  $g_n \cdots g_1$  represent the same polynomial automorphism g if and only if n = m and there exist maps  $s_i \in \mathcal{S}$ ,  $i = 0, \ldots, m$  such that  $s_0 = s_m = id$  and  $g_i = s_i g_i s_{i-1}^{-1}$ .

From this theorem it follows that

A. Gómez, J.D. Meiss / Physics Les

To prove the second part of the proposition, consider first a linear, nonelementary involution a(x, y). In that case, taking s(x, y) = x(1, 0) + ya(1, 0), we see that  $a = sts^{-1}$ .

Next, we show that every affine, nonelementary involution (12) is  $\mathfrak E$ -conjugate to its linear part a. We know that  $(\ ,\ )=(a-id)(c,0)$  for some scalar c. Taking s(x,y)=(x+c,y) it follows that  $sas^{-1}=a$  and the proof is complete.  $\square$ 

## 3.2. Normal forms

We intend to d

**Proof.** Consider g given by the reduced word (14

A. Gómez, J.D. Meiss / Physics Letters A 312 (