- 1. (34 points) Find the requested information. The problems are unrelated.
  - (a) Evaluate  $\frac{\tan^{-1}(x)}{x^2}$  dx (Hint: Start with IBP)
  - (b) Findy as a function  $\otimes$  fgiven that  $\frac{dy}{dx} = 2x^p \frac{1-y^2}{1-y^2}$  and y(0) = 1
  - (c) Find the sum of the series  $\frac{x^6}{5!} + \frac{x^{10}}{5!} \frac{x^{14}}{7!} + \cdots$
  - (d) For what values of ones the series  $\sin^2(\cdot)\cos^{2n}(\cdot)$  converge? Find the sum for those values of  $\cos^{2n}(\cdot)$
- 2. (16 points) Decide whether the following quantities are convergent or divergent. Explain your reasoning a any test you use.
  - (a) The sequence given  $\frac{dy}{dy} = 1 \frac{\ln(3)}{n}^n$ , for n = 1; 2:::

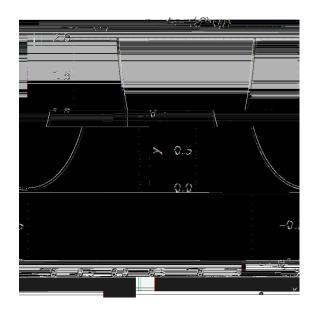
(b) 
$$\begin{bmatrix} Z_1 & r \\ \frac{1}{x^2} & 1 + \frac{3}{x^3} dx \end{bmatrix}$$

- 3. (12 points) Consider the series, Suppose the partial sum of the series, is  $2 \frac{2}{n+1}$ .
  - (a) What is<sub>3</sub>?
  - (b) Find a simple formula for
  - (c) What  $does _n g$  converge to?
  - (d) What is the sum of the seriets?
- 4. (25 points) Recadsh(x) =  $\frac{e^{x} + e^{-x}}{2}$ .
  - (a) Find the MacLaurin series of the hyperbolic cosine function.
  - (b) Find the interval of convergence for the power series from part (a).
  - (c) FindT<sub>3</sub>(x), the Taylor polynomial of order 3, of the hyperbolic cosine ceater@d be the Taylor Remainder formula to nd an upper bound for the absolute@xnos if sed to approximatesh(1)
  - (d) Use the MacLaurin series (nooplital!) to evaluate the following limit:

$$\lim_{x! = 0} \frac{\cosh(x) - 1 - \frac{x^2}{2}}{x^4}$$
:

- 5. (18 points) Suppose) equals the power series  $\frac{x!}{c^{2n}}$ , wherebandcare constants, and the series has an interval of convergence of < 2
  - (a) Find the center and radius of convergence of the series.

- (b) Evaluate g(x) dx as a power series.
- (c) Given the interval of convergence, nd possible valbasdor Justify your answer using appropriate test(s).
- 6. (25 points) For this problem, +etan() for -2 < < 2 The polar graph (in the plane) is given below. Answer the following questions.



(a) Find an equation for the tangent line at 4.