- 1. (28 points) The following problems are not related.
 - (a) Find the general antiderivative of $g(x) = \frac{e^{\rho_{\overline{x}}}}{\varphi_{\overline{x}}}$.
 - (b) Use logarithmic differentiation to find the derivative of $y = (x^4 + 1)^x$. You do not need to simplify your answer.
 - (c) Find the derivative of $f(x) = \frac{Z \cos(x) p}{1 + t^3} dt$.
- 2. (26 points) The following problems are not related:
 - (a) Find the derivative of $f(x) = \ln \tan^{-1}(x)$.
 - (b) Evaluate the definite integral $Z_{ln(3)}$ $\sinh(x) \cosh(x) dx$, and fully simplify your answer.
 - (c) Determine the value of the limit $\lim_{x/=0^+} x^2 \ln(x^2)$.
- 3. (16 points) Find the area of the largest rectangle which is symmetric around the y-axis, bounded below by the x-axis, and which has two corners touching the graph of $f(x) = \frac{1}{1+x^2}$. Fully justify your answer by using an appropriate test.

5. (12 points) For what value of a is the following function continuous?

$$f(x) = \begin{cases} 8 \\ \ge 2x^2 & x + a; \quad x = 0 \end{cases}$$

$$f(x) = \begin{cases} \frac{x}{2\sin(x)}, & x > 0 \end{cases}$$

Justify your answer with appropriate computations.

6. (18 points) Consider the function

$$g(x) = \arctan(x) + \frac{1}{x^2 - 4}$$

- (a) Find the domain of the function, and give your answer in interval notation.
- (b) Find all horizontal asymptotes of g(x), and justify your answer with limits.
- 7. (16 points) The half-life of the chemical element cobalt-56 is approximately 77 days. Suppose we have a 10 milligram sample of cobalt-56..
 - (a) Find a formula for the mass of cobalt-56 remaining after *t* days.
 - (b) How long will it take for only 1 milligram of cobalt-56 to remain in the sample? *It is OK for your answer to have a logarithm in it.*
- 8. (16 points) For each of the following questions, give a short justification for your answer.

(a) If
$$f(x)$$
 is an odd function and $\int_{3}^{Z} f(x) dx = \int_{3}^{Z} f(x) dx$.

(a)

) is an odd function and