1. (24 points) The following problems are not related. If a limit does not exist, you must say so. If you use a theorem, clearly state its name and show that its hypotheses are satisfied.
   (Reminder: You may not use L'Hôpital's Rule or "Dominance of Powers" in any solutions on this exam.)

   (a) $\lim_{x \to 0} \dfrac{\sec x}{4x \cot 2x}$

   (b) $\lim_{x \to 1} \dfrac{\sin^2 x}{x}$

   (c) $\lim_{x \to 1} \dfrac{x - 1}{2 - \sqrt{5 - x^2}}$

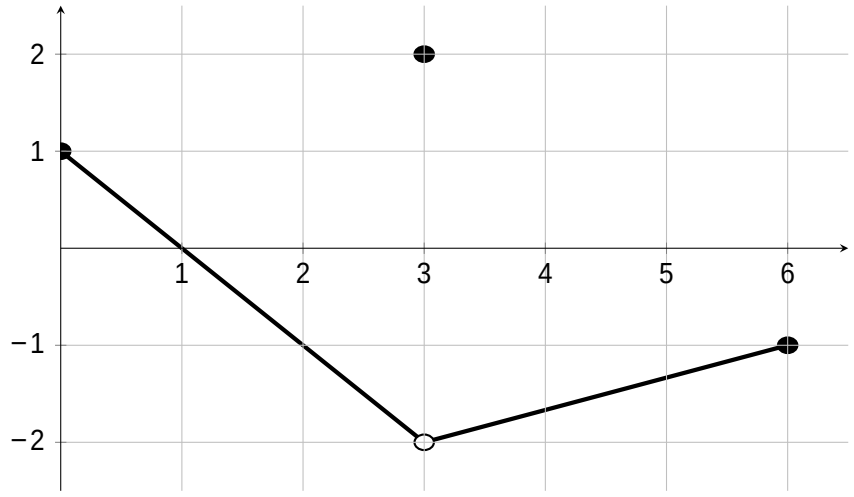
2. (21 points) The following problems are unrelated.

   (a) Given that csc $= \sqrt{5}$ and $=2 <$ $<$, find the values of tan and cos(2).

   (b) Find all values of x in the interval [0;] that satisfy $\tan x \sec x = 4 \sin x$.

   (c) A squirrel is up a tree, and it sees a peanut on the ground some distance away. If the straight-line distance between the peanut and the squirrel is 50 ft, and the angle between the straight-line and the tree is =6 radians, how far down the tree and across the ground must the squirrel travel to reach the peanut? *Give your answer with appropriate units.*

3. (15 points) Shown below is a graph of $y = f(x)$, which consists of two line segments with a single removable discontinuity.



   (a) Find a formula for $f(x)$.

   (b) Sketch a graph of $y = |f(x)| + 1$. Label the intercepts, if any.

   (c) Suppose we use the precise definition of a limit to verify the value of $\lim_{x \to 5} f(x)$, and we find that if $4 < x < 6$, then $-\frac{5}{3} < f(x) < -1$. What are the corresponding values of and ? (recall the precise definition of a limit: *the limit of $f(x)$ as x approaches a is L if for every number > 0, there is a corresponding > 0 such that if $0 < |x - a| <$, then $|f(x) - L| <$.*

4. (20 points) Consider the function $g(x) = \dfrac{2x^2 - 12x + 16}{x^2 - 7x + 12}$.